

ON STOCHASTIC APPROXIMATION METHODS IN SYSTEMS ANALYSIS

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Abstract

From some time past our interest was focused to find new possibilities for characterizing the process of generation of the words by generative systems. In our previous papers [4] and [5] we have introduced some numerical functions able to characterize classes of derivations according to a given generative system (as the phrase-structure grammars known in formal languages) up to an equivalence. They are referred to as "derivational functions". In this paper we consider equivalence classes of derivation and we establish some new properties of symmetry and invariance. A like limit theorem result is also obtained.

On the other hand it is known that a precise definition of the Brownian motion involves a measure on the path space, such that it is possible to put the Brownian motion on a firm mathematical foundation. Much scientific work has been done on its applications in such diverse areas as molecular and atomic physics, chemical kinetics, solid-state theory, stability of structures, population genetics, communications, and many other branches of the natural and social sciences and engineering.

In the last part of this paper we refer to an application of asymptotic theory of stochastic differential equation in mathematical genetics ([7], [8], [10]).

Keywords. Brownian motion, stochastic differential equation, Markov processes, transition probabilities.

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