

# On a 9-dimensional family of Naturally Graded non $p$ -filiform Lie Algebras \*

L.M. Camacho<sup>†</sup>      J.R. Gómez<sup>†</sup>      A.J. González<sup>†</sup>

February 13, 2004

## Abstract

The knowledge of the naturally graded algebras among those of a given class of Lie algebras offers essential information about the structure of the class.

So far, the classification of naturally graded Lie algebras is only known for some families of  $p$ -filiform Lie algebras [4], [2], [1]. In certain sense, if  $\mathfrak{g}$  is a naturally graded Lie algebra of dimension  $n$ , the first case of non  $p$ -filiform Lie algebras occurs when the characteristic sequence is  $(n-3, 2, 1)$ . We offer the classification of these algebras in dimension 9. There is a technical parameter,  $r$ , which in this case must be  $r = 1, 3, 5$ . For  $r = 1$ , we obtain two pairwise non isomorphic Lie algebras (this case is solved in arbitrary finite dimension [3]). For  $r = 5$  there is one single algebra. The most difficult case is for  $r = 3$ . We obtain two pairwise non isomorphic Lie algebras and an uniparameter family of pairwise non isomorphic Lie algebras of laws  $\mu(\alpha)$  where  $\mu(\alpha) \simeq \mu(\alpha')$  if  $\alpha' = \pm\alpha$  or  $\alpha' = \pm i\sqrt{\frac{4+3\alpha^2}{3+2\alpha^2}}$ .

## References

- [1] J.M. Cabezas, J.R. Gómez, E. Pastor, *Naturally graded 3-filiform Lie algebras*, submitted to Journal of Pure and Applied Algebra.
- [2] J.R. Gómez, A. Jiménez-Merchán, *Naturally graded quasifiliform Lie algebras*, Journal of Algebra, 256, 211-228, 2002.
- [3] A.J. González, *Graduaciones naturales de una familia de álgebras de Lie no  $p$ -filiforme*, Minor Thesis, University of Seville, 2003.
- [4] M. Vergne, *Cohomologie des algèbres de Lie nilpotentes. Application à l'étude de la variété des algèbres de Lie nilpotentes*, Bull. Soc. Math. France, 98, 81-116, 1970.

---

\*This paper has been partially supported by the PAICYT, of Junta de Andalucía (Spain), and by the Ministerio de Ciencia y Tecnología (Spain), ref. BFM 2000-1047

<sup>†</sup>Dpto. Matemática Aplicada I. Univ. Sevilla. Avda. Reina Mercedes S.N. 41012 Sevilla (Spain). E-mail: lcamacho@us.es - jrgomez@us.es - agonzalez@us.es