

11.1.12.

$$1, \cos \frac{n\pi x}{p}, \sin \frac{m\pi x}{p}, \quad n = 1, 2, 3, \dots, m = 1, 2, 3, \dots; \quad [-p, p].$$

$$\left(1, \cos \frac{n\pi x}{p}\right) = \int_{-p}^p 1 \cos \frac{n\pi x}{p} dx = \left[ \frac{p}{n\pi} \sin \frac{n\pi x}{p} \right]_{-p}^p = 0$$

$$\left(1, \sin \frac{m\pi x}{p}\right) = \int_{-p}^p 1 \sin \frac{m\pi x}{p} dx = \left[ \frac{-p}{m\pi} \cos \frac{m\pi x}{p} \right]_{-p}^p = 0$$

$$(1, 1) = \int_{-p}^p 1 \cdot 1 dx = 2p$$

$n \quad m$

$$\left(\cos \frac{n\pi x}{p}, \sin \frac{m\pi x}{p}\right) = \frac{1}{2} \sin \frac{(m-n)\pi x}{p} + \sin \frac{(m+n)\pi x}{p} dx = 0$$

$n = m$

$$\left(\cos \frac{n\pi x}{p}, \sin \frac{n\pi x}{p}\right) = \frac{1}{2} \sin \frac{2n\pi x}{p} dx = 0$$

$n \quad m$

$$\left(\cos \frac{n\pi x}{p}, \cos \frac{m\pi x}{p}\right) = \frac{1}{2} \cos \frac{(m-n)\pi x}{p} + \cos \frac{(m+n)\pi x}{p} dx = 0$$

$$n = m$$

$$\left(\cos \frac{n\pi x}{p}, \cos \frac{n\pi x}{p}\right) = \frac{1}{2} \int_{-p}^p \left(1 + \cos \frac{2n\pi x}{p}\right) dx = p$$

$$n \neq m$$

$$\left(\sin \frac{n\pi x}{p}, \sin \frac{m\pi x}{p}\right) = \frac{1}{2} \int_{-p}^p \left(\cos \frac{(m-n)\pi x}{p} - \cos \frac{(m+n)\pi x}{p}\right) dx = 0$$

$$n = m$$

$$\left(\sin \frac{n\pi x}{p}, \sin \frac{n\pi x}{p}\right) = \frac{1}{2} \int_{-p}^p \left(1 - \cos \frac{2n\pi x}{p}\right) dx = p$$

$$\text{Normerna : } \left| \cos \frac{n\pi x}{p} \right| = \left| \sin \frac{n\pi x}{p} \right| = \sqrt{p}, \quad \|1\| = \sqrt{2p}.$$