

11.2.20.

$$\frac{\pi}{4} = \frac{1}{2} + \frac{1}{1 \cdot 3} - \frac{1}{3 \cdot 5} + \frac{1}{5 \cdot 7} - \frac{1}{7 \cdot 9} + \dots$$

Visas !

$$\frac{\pi}{4} = \frac{1}{2} + \sum_{m=1}^{\infty} \frac{-(-1)^m}{(2m-1)(2m+1)}$$

$$f(x) = \begin{cases} 0 & , \quad -\pi < x < 0 \\ \sin x & , \quad 0 < x < \pi \end{cases}$$

$$f \sim \frac{1}{\pi} + \frac{1}{2} \sin x - \sum_{n=2}^{\infty} \frac{1 + (-1)^n}{\pi(n^2 - 1)} \cos nx$$

$$\sin \frac{\pi}{2} = f\left(\frac{\pi}{2}\right) = \frac{1}{\pi} + \frac{1}{2} \sin \frac{\pi}{2} - \sum_{n=2} \frac{1 + (-1)^n}{\pi(n^2 - 1)} \cos \frac{n\pi}{2}$$

$$\cos \frac{n\pi}{2} = \begin{cases} 0, & n = 2m + 1 \\ (-1)^m, & n = 2m \end{cases}$$

$$\frac{\pi}{2} = 1 - \sum_{m=1} \frac{2}{(2m)^2 - 1} (-1)^m$$

$$\frac{\pi}{4} = \frac{1}{2} - \sum_{m=1} \frac{(-1)^m}{\pi((2m)^2 - 1)}$$