

7.1.4.

$$f(t) = \begin{cases} 2t + 1, & 0 \leq t < 1 \\ 0, & t \geq 1 \end{cases}$$

$$L\{f(t)\} = \int_0^{\infty} e^{-st} f(t) dt$$

$$L\{f(t)\} = \int_0^1 e^{-st} (2t + 1) dt + \int_1^{\infty} e^{-st} 0 dt =$$

$$= \left[(2t + 1) \frac{e^{-st}}{-s} \right]_0^1 - \left[\frac{e^{-st}}{-s} \right]_0^1 2dt =$$

$$= \frac{1 - 3e^{-s}}{s} - \left[2 \frac{e^{-st}}{s^2} \right]_0^1 = \frac{1 - 3e^{-s}}{s} + 2 \frac{1 - e^{-s}}{s^2}$$