

7.2.30.

$$L^{-1} \frac{6s + 3}{s^4 + 5s^2 + 4} = L^{-1} \frac{6s + 3}{(s^2 + 1)(s^2 + 4)} =$$

$$= L^{-1} \frac{As + B}{s^2 + 1} + \frac{Cs + D}{s^2 + 4} =$$

$$\begin{aligned} 6s + 3 &= (As + B)(s^2 + 4) + (Cs + D)(s^2 + 1) \\ s^3: 0 &= A + C, & C &= -A \\ s^2: 0 &= B + D, & D &= -B \\ s: 6 &= 4A + C, & 6 &= 3A \\ s^0: 3 &= 4B + D, & 3 &= 3B \end{aligned}$$

$$= L^{-1} \frac{2s + 1}{s^2 + 1} + \frac{-2s - 1}{s^2 + 4} =$$

$$= 2L^{-1} \frac{s}{s^2 + 1} + L^{-1} \frac{1}{s^2 + 1} - 2L^{-1} \frac{s}{s^2 + 4} - L^{-1} \frac{1}{s^2 + 4} =$$

$$= 2 \cos t + \sin t - 2 \cos 2t - \frac{1}{2} \sin 2t$$