

7.6.6.

$$x' + x - y' + y = 0 \quad x(0) = 0$$

$$x' + y' + 2y = 0 \quad y(0) = 1$$

$$sX(s) - 0 + X(s) - (sY(s) - 1) + Y(s) = 0$$

$$sX(s) - 0 + (sY(s) - 1) + 2Y(s) = 0$$

$$(s + 1)X(s) - (s - 1)Y(s) = -1$$

$$sX(s) + (s + 2)Y(s) = 1$$

$$\begin{array}{ccc} s + 1 & -(s - 1) & X(s) \\ s & s + 2 & Y(s) \end{array} = \begin{array}{c} -1 \\ 1 \end{array}$$

$$X(s) = \frac{\begin{vmatrix} -1 & -(s - 1) \\ 1 & s + 2 \end{vmatrix}}{\begin{vmatrix} s + 1 & -(s - 1) \\ s & s + 2 \end{vmatrix}} = \frac{-3}{2s^2 + 2s + 2}$$

$$Y(s) = \frac{\begin{vmatrix} s + 1 & -1 \\ s & 1 \end{vmatrix}}{\begin{vmatrix} s + 1 & -(s - 1) \\ s & s + 2 \end{vmatrix}} = \frac{2s + 1}{2s^2 + 2s + 2}$$

$$X(s) = \frac{-3}{2(s^2 + s + 1)} = \frac{-\sqrt{3}\sqrt{3}}{2\left(\left(s + \frac{1}{2}\right)^2 + \frac{3}{4}\right)}$$

$$Y(s) = \frac{2s + 1}{2(s^2 + s + 1)} = \frac{s + \frac{1}{2}}{\left(\left(s + \frac{1}{2}\right)^2 + \frac{3}{4}\right)}$$

$$x(t) = -\sqrt{3}e^{-\frac{t}{2}} \sin \frac{t\sqrt{3}}{2}$$

$$y(t) = e^{-\frac{t}{2}} \cos \frac{t\sqrt{3}}{2}$$