

10.18.

$$\mathbf{u} = f(x) (x^2 + y^2 + z^2)$$

$$\mathbf{u} = f(x)(2x, 2y, 2z)$$

$$\operatorname{div} \mathbf{u} = 2 \frac{\partial}{\partial x} \{f(x)x\} + \frac{\partial}{\partial y} \{f(x)y\} + \frac{\partial}{\partial z} \{f(x)z\}$$

$$\operatorname{div} \mathbf{u} = 2 \{ f(x)x + f(x) + f(x) + f(x) \}$$

Källfritt : $\operatorname{div} \mathbf{u} = 0$.

$$f(x)x + 3f(x) = 0$$

$$f(x)x^3 + 3x^2 f(x) = 0$$

$$\frac{d}{dx} \{ x^3 f(x) \} = 0$$

$$x^3 f(x) = C$$

SVAR: Källfritt vektorfält då $f(x) = \frac{C}{x^3}$.