

- 1: Recall the definition of curvature and torsion (of a curve in \mathbb{R}^3 , via/in arc-length parametrization).
- 2: Prove the reparametrization invariance of $\kappa = -\frac{1}{\rho} |\dot{\vec{r}} \ddot{\vec{r}} \ddot{\vec{r}} \ddot{\vec{r}}| / |\dot{\vec{r}}|^3 = |\dot{\vec{r}} \ddot{\vec{r}} \ddot{\vec{r}} \ddot{\vec{r}}| / (\dot{\vec{r}} \times \ddot{\vec{r}})^2$
- 3: Calculate κ and τ for a helix, $\vec{r}(t) = (a \cos t, a \sin t, bt)$.
- 4: Find a polynomial (of degree 2 in x^2, y^2 and z^2) such that $P \equiv 0$ describes the 2-torus, $((a + b \cos u) \cos v, (a + b \cos u) \sin v, b \sin u)$.
- 5: Convert the 2-sphere via 2 stereographic projections and calculate the transition functions.
- 6: Prove non-orientability of the Möbius-strip $((2 - v \sin(u/2)) \sin u, (2 - v \sin(u/2)) \cos u, v \cos(u/2))$.
- 7: Calculate the distance between north- and south-pole of S^2 using the first fundamental form in stereographic projection parametrization.
- 8: Prove reparametrization invariance of $A = \int_M \Omega$ under
- 9: Calculate the principal curvatures of the helicoid, from $\vec{X}(u, v) = (b \sin u \cos v, b \sin u \sin v, v)$