

908.g.

$$V = \int_{y=0}^1 \left(\int_{x=y}^{2y} \frac{y dx}{1+x^3} \right) dy + \iint_D \frac{y dx dy}{1+x^3}$$

$$D = \{(x, y) : 1 \leq y \leq x, 1 \leq x \leq 2\}$$

$$V = \int_{x=0}^2 \left(\int_{y=x/2}^x \frac{y dy}{1+x^3} \right) dx = \int_{x=0}^2 \frac{1}{2} \frac{y^2}{1+x^3} \Big|_{y=x/2}^x dx$$

$$V = \int_{x=0}^2 \frac{1}{8} \frac{3x^2}{1+x^3} dx = \frac{1}{8} \left[\ln(1+x^3) \right]_{x=0}^2 = \frac{1}{8} \ln 9 = \frac{1}{4} \ln 3$$