

927.j.

$$\begin{cases} x^2 + y^2 = a^2 \\ x^2 + z^2 = a^2 \end{cases}, \quad a > 0$$

$$V = \int_K dx dy dz$$

$$V = \int_{D_{xy}} \left(\int_{z = -\sqrt{a^2 - x^2}}^{\sqrt{a^2 - x^2}} dz \right) dx dy = 2 \int_{D_{xy}} \sqrt{a^2 - x^2} dx dy$$

$$V = 2 \int_{x=-a}^a \left(\int_{y=-\sqrt{a^2 - x^2}}^{\sqrt{a^2 - x^2}} \sqrt{a^2 - x^2} dy \right) dx = 8 \int_{x=0}^a (a^2 - x^2) dx = \frac{16a^3}{3}$$

927.m.

$$z^2 = x^2 + y^2$$

$$x^2 + y^2 + z^2 = 2, \quad z \geq 0$$

$$V = \int_K dx dy dz$$

$$x = r \sin \theta \cos \phi$$

$$y = r \sin \theta \sin \phi$$

$$z = r \cos \theta$$

$$K_{r\theta\phi} = \{(r, \theta, \phi) : 0 \leq r \leq \sqrt{2}, 0 \leq \theta \leq \frac{\pi}{4}, 0 \leq \phi < 2\pi\}$$

$$dx dy dz = \left| \det \left(\frac{d(x, y, z)}{d(r, \theta, \phi)} \right) \right| dr d\theta d\phi = r^2 \sin \theta dr d\theta d\phi$$

$$V = \int_{K_{r\theta\phi}} r^2 \sin \theta dr d\theta d\phi$$

$$V = 2\sqrt{2} \int_{r=0}^{\frac{\sqrt{2}}{4}} r^2 dr \int_{\theta=0}^{\frac{\pi}{4}} \sin \theta d\theta$$

$$V = 2\sqrt{2} \frac{2\sqrt{2}}{3} \left(1 - \frac{1}{\sqrt{2}} \right) = \frac{4\sqrt{2}}{3} (\sqrt{2} - 1)$$