

938.c.

$$V = \iint_D \frac{\sin x}{(x^2 + y^2)^{3/2}} dx dy$$

$$D = \{(x, y) : x^2 + y^2 \geq 1\}$$

$$|V| \leq \iint_D \frac{|\sin x|}{(x^2 + y^2)^{3/2}} dx dy \leq \iint_D \frac{1}{(x^2 + y^2)^{3/2}} dx dy$$

$$\iint_D \frac{1}{(x^2 + y^2)^{3/2}} dx dy = \begin{cases} x = r \cos v \\ y = r \sin v \\ D_{rv} = \{(r, v) : 1 \leq r, 0 \leq v \leq 2\pi\} \end{cases} \quad \begin{matrix} dx dy = r dr dv \\ \\ \\ \end{matrix} = \iint_{D_{rv}} \frac{r dr dv}{r^3}$$

$$\iint_D \frac{1}{(x^2 + y^2)^{3/2}} dx dy = 2 \int_0^{\pi} \int_1^{\infty} \frac{1}{r^3} r dr d\theta = 2 \int_0^{\pi} \left[-\frac{1}{2r^2} \right]_{r=1}^{\infty} d\theta = 2 \int_0^{\pi} \frac{1}{2} d\theta = \pi$$

$$|V| = \pi$$

Integralen $V = \iint_D \frac{\sin x}{(x^2 + y^2)^{3/2}} dx dy$ är konvergent.