

LS5. Version B.

$$x^2 y'' + 2xy' - 6y = 0$$

$$y = x^3 z$$

$$y' = x^3 z' + 3x^2 z, \quad y'' = x^3 z'' + 6x^2 z' + 12x z$$

$$x^2 \left\{ x^3 z'' + 6x^2 z' + 12x z \right\} +$$
$$+ 2x \left\{ x^3 z' + 3x^2 z \right\} - 6x^3 z = 0$$

$$x^4 z'' + 4x^3 z' = 0$$

$$u = z', \quad u' = z''$$

$$u'' - 4x^{-1}u = 0$$

$$x^{-4}u'' - 4x^{-5}u = 0$$

$$(x^{-4}u)' = 0 \quad u = C_1 x^4 = z'$$

$$z = C_3 x^5 + C_2$$

$$y = x^{-3}z = C_3 x^2 + C_2 x^{-3}$$

$$y_2 = x^2$$

$$W(x^{-3}, x^2) = \begin{vmatrix} x^{-3} & x^2 \\ -3x^{-4} & 2x \end{vmatrix} = 5x^{-2} \neq 0$$

x^{-3} och x^2 är linjärt oberoende .