

```
[ > with(orthopoly):
[ >
[ > ((2*n+1)/2) * int( exp(x)*P(n,x) , x=-1..1);

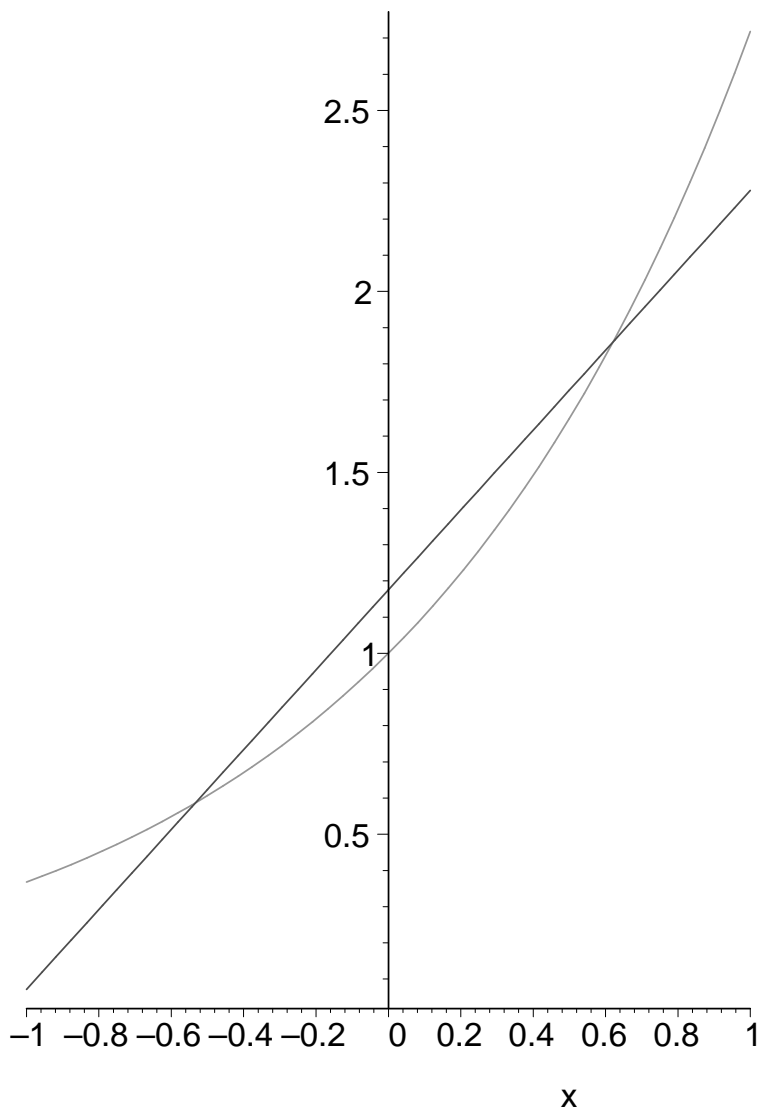
$$\frac{1}{2}(2n+1) \int_{-1}^1 e^x P(n,x) dx$$

[ > sum('((2*n+1)/2) * int( exp(x)*P(n,x) , x=-1..1) *
P(n,x)', 'n'=0..1); evalf(%);

$$\frac{1}{2}e - \frac{1}{2}e^{(-1)} + 3e^{(-1)}x$$


$$1.175201193 + 1.103638324x$$

[ > plot(
[sum('((2*n+1)/2) * int( exp(x)*P(n,x) , x=-1..1) *
P(n,x)', 'n'=0..1) , exp(x)]
, x=-1..1);
```



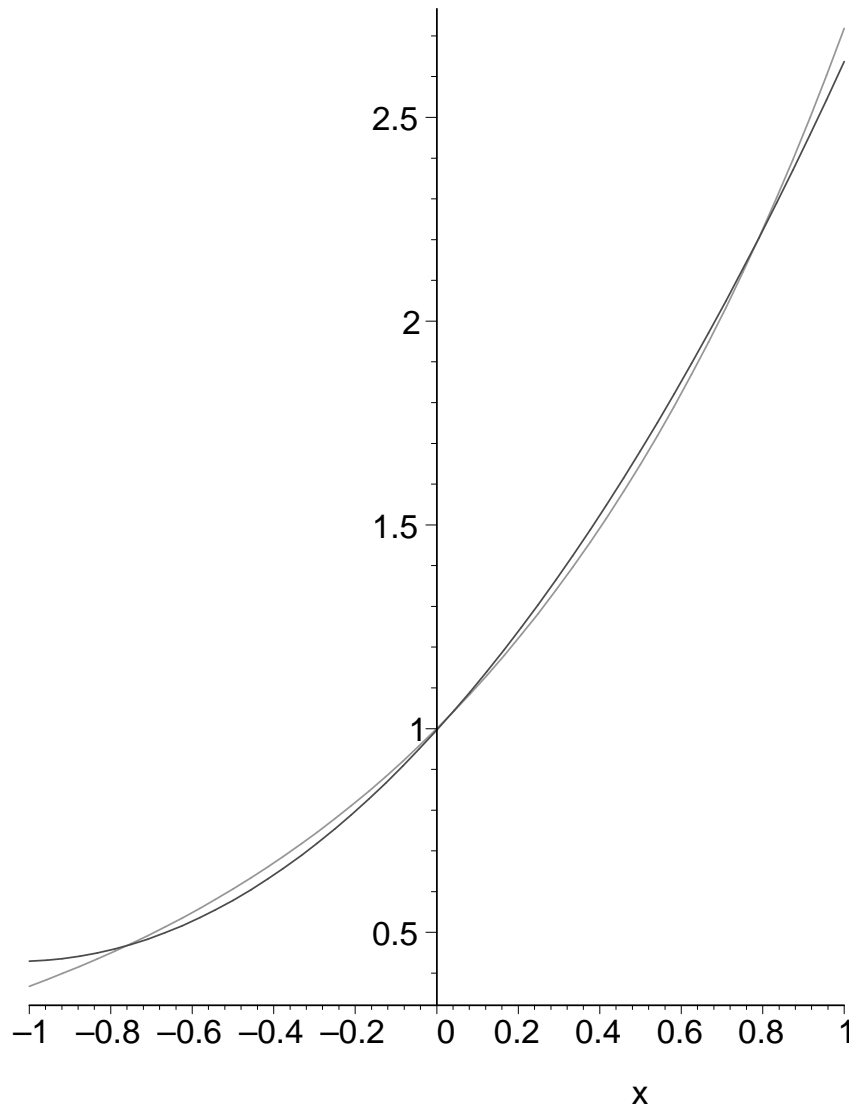
```
[ > sum('((2*n+1)/2) * int( exp(x)*P(n,x) , x=-1..1) *
```

```
P(n,x)', 'n'=0..2); evalf(%);
```

$$\frac{1}{2}e - \frac{1}{2}e^{(-1)} + 3e^{(-1)}x + \frac{5}{2}(e - 7e^{(-1)})\left(-\frac{1}{2} + \frac{3x^2}{2}\right)$$

$$0.9962940180 + 1.103638324x + 0.5367215250x^2$$

```
> plot(
[sum('((2*n+1)/2) * int( exp(x)*P(n,x) , x=-1..1) *
P(n,x)', 'n'=0..2) , exp(x)]
, x=-1..1);
```



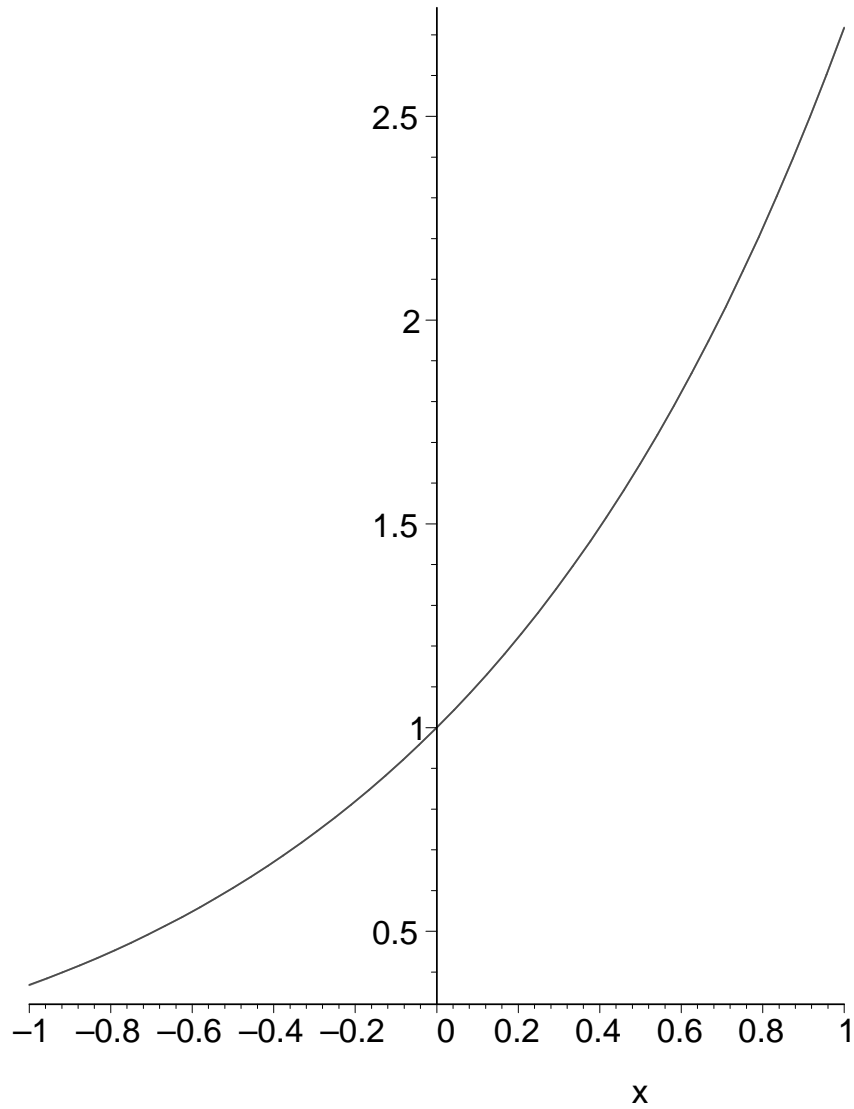
```
> sum('((2*n+1)/2) * int( exp(x)*P(n,x) , x=-1..1) *
P(n,x)', 'n'=0..4); evalf(%);
```

$$\frac{1}{2}e - \frac{1}{2}e^{(-1)} + 3e^{(-1)}x + \frac{5}{2}(e - 7e^{(-1)})\left(-\frac{1}{2} + \frac{3x^2}{2}\right) + \frac{7}{2}(-5e + 37e^{(-1)})\left(\frac{5}{2}x^3 - \frac{3}{2}x\right)$$

$$+ \frac{9}{2}(36e - 266e^{(-1)})\left(\frac{3}{8} + \frac{35}{8}x^4 - \frac{15}{4}x^2\right)$$

$$1.000030902 + 0.9979548790x + 0.4993526812x^2 + 0.1761390750x^3 + 0.04359698438x^4$$

```
> plot(  
[sum('((2*n+1)/2) * int( exp(x)*P(n,x) , x=-1..1) *  
P(n,x)', 'n'=0..4) , exp(x)]  
, x=-1..1);
```



```
[ >
```