

$$\pi_i = \frac{1}{E(T_i)}$$

$\frac{\pi_j}{\pi_i}$  = E(ANTAL BESÖK i  
 j MELLAN 2  
 BESÖK i i)

2

|  | 1 | 2 | 3 |
|--|---|---|---|
|  | 0 | 0 | 0 |
|  | 0 | 0 | 1 |
|  | 0 | 1 | 0 |
|  | 0 | 1 | 0 |
|  | 1 | 0 | 0 |
|  | 1 | 0 | 1 |
|  | 1 | 1 | 0 |
|  | 1 | 1 | 1 |

0 = 'TRASIG'  
1 = 'HEL'

GER Q

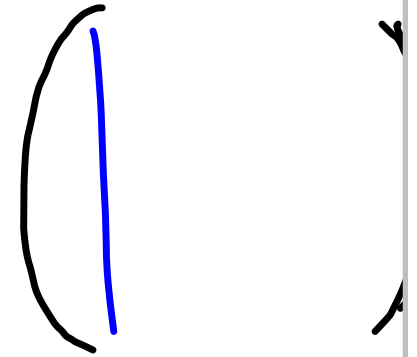
$$\underline{0} = \underline{\pi} Q$$

$$\begin{cases} \underline{0} = \underline{\Pi} Q \\ \sum_{\lambda \in E} \pi_{\lambda} = 1 \end{cases}$$

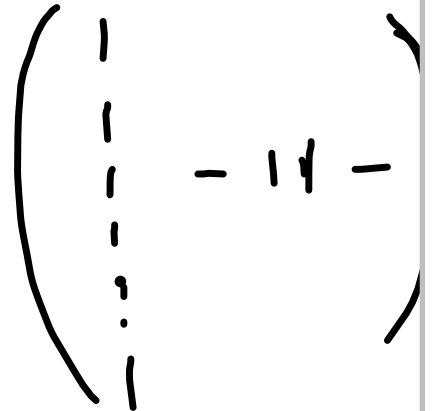
$$\underline{\Pi} = (\dots\dots)$$

стык

$$(\cancel{0}, 0, \dots, 0) = (\dots\dots)$$



$$(1, 0, \dots, 0) = \underbrace{(\dots\dots)}_{\underline{\Pi}} \cdot \left( \begin{array}{c} - \\ - \\ - \\ \vdots \\ - \\ - \\ - \end{array} \right)$$



KENDALL

BETJÄNINGSTIDSFÖRDELN.  
M = MARKOVIAN; EXP-FÖRD.

D = DETERMINISTISK

G = GENERAL

A/B/c/K

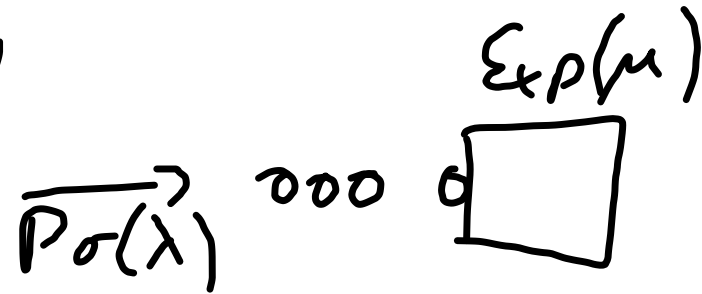
↓  
VÄNTNUM

↑  
ANKOMSTPROCESS

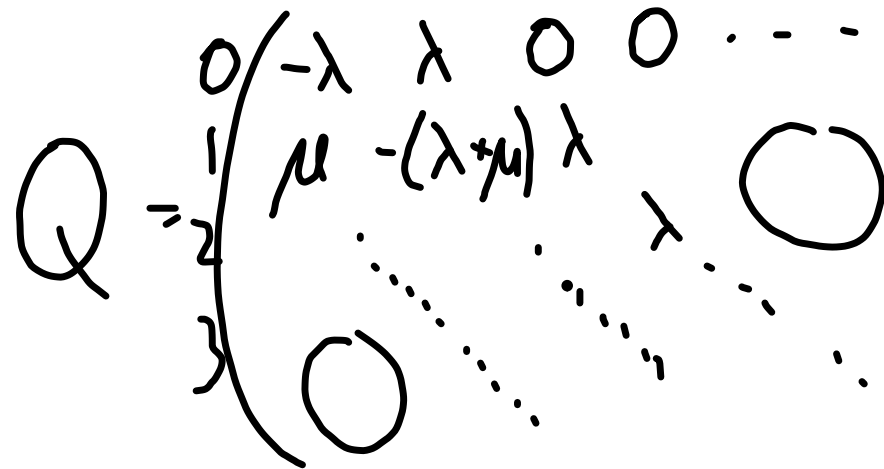
M = MARKOVIAN : POISSONPROCESS

ANTAL PARALLELLA BETJ. STN

M/M/1



$\bar{X}(t) = \lambda / \mu < 1$   
i SYSTEMET



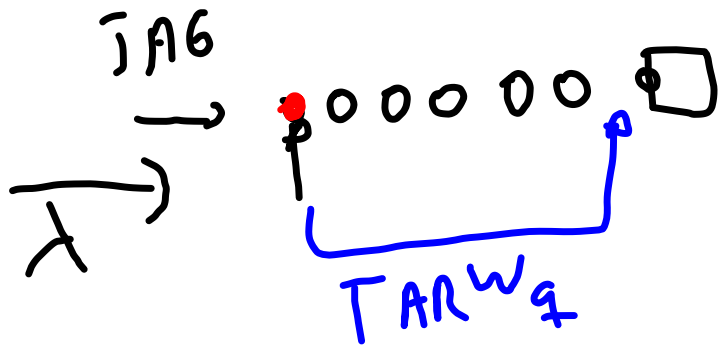
$\rho = \frac{\lambda}{\mu} < 1$   
TRAFIK-  
INTENSITET

$$P_n = (1 - \rho) \rho^n \quad n = 0, 1, 2, \dots$$

$$L = \sum_{n=0}^{\infty} n \cdot P_n$$

$$L_q = 0 \cdot P_0 + 0 \cdot P_1 + 1 \cdot P_2 + 2 \cdot P_3 + \dots$$

$$W_q = \frac{l_q}{\lambda}$$



HAR KOMMIT UNDER MIN KÖTID  
 $\approx W_q$

$$\lambda \cdot W_q = l_q$$

$$C = 1$$

$$P_0 = 1 - \rho$$

$$\underbrace{1 - P_0}_{\rho} = \rho$$

P(BETJÄNING PÅGÅR)

$$\rho = E(\text{ANTAL BETJ.})$$

$$\underbrace{l}_{E(\text{SYST.})} = \underbrace{\rho}_{E(\text{BETJ.})} + \underbrace{l_q}_{E(\text{KÖN})}$$

$$\rho = \frac{\lambda}{c\mu} < 1$$

ALLMÄNT  $l = c\rho + l_q$

$$\frac{l}{\lambda} = \frac{c\rho}{\lambda} + \frac{l_q}{\lambda} = \underbrace{\frac{1}{\mu} + \frac{w_q}{\lambda}}_w$$

$$\underline{\Pi} = \underline{\Pi} P$$

$$\underline{Q} = \underline{\Pi} (\underline{I} - P)$$

$$(1, 0, 0, \dots) = \underbrace{(\dots)}_{\underline{\Pi}}$$

$$\left( \begin{array}{c} | \\ | \\ | \\ \vdots \end{array} \right)$$

$\underline{I} - P$  RESTEN  
UTOM KOLUMN 1



M/G/1

↑  
ALLMÄN BETJ. TIDSFÖRD

BETRAKTA ANTAL I SYSTEMET

PRECIS DÅ KUND LÄMNAR SYSTEMET.

SPEC. FALL

M/M/1

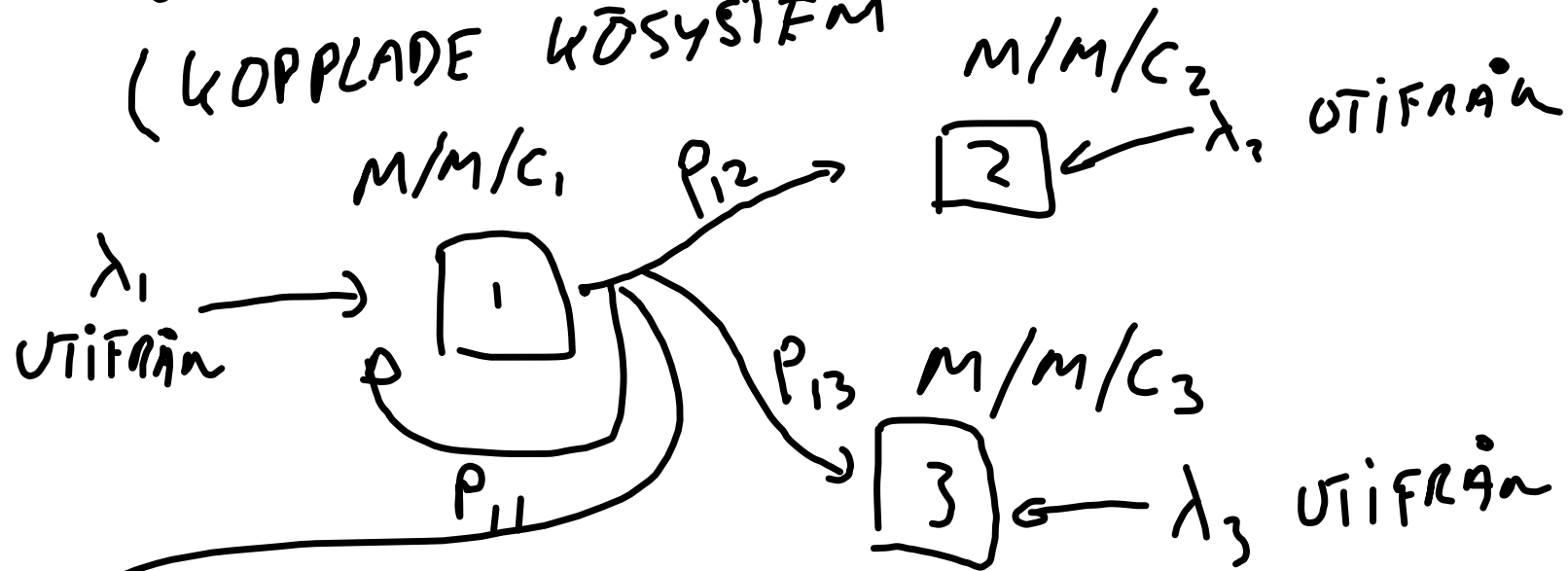
$$V(u) = \frac{1}{\lambda^2} \quad E(u) = \frac{1}{\lambda}$$

$$l_q = \frac{\rho^2}{2(1-\rho)} (1 + 1) = \frac{\rho^2}{1-\rho} = l_q$$

FRÅN

⇒  $l, w, w_q$  VIA LITTLE'S FORMLER FS OM M/M/1

# JACKSON-NÄTVERK (KOPPLADE KÖSYSTEM)



$$P_i = 1 - P_{i1} - P_{i2} - P_{i3} = P(\text{GÅ HEM FRÅN NOD } i)$$

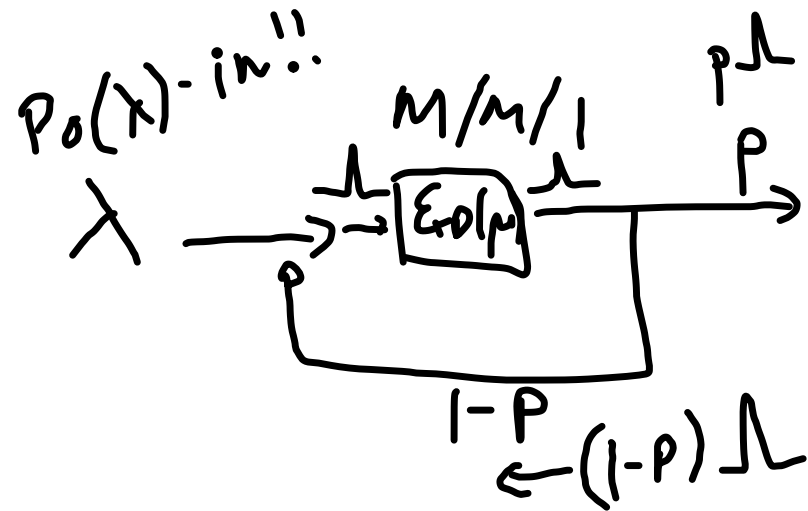
$$L_1 = \lambda_1 + P_{11} \cdot L_1 + P_{21} \cdot L_2 + P_{31} \cdot L_3$$

TOTALT FLÖDE IN I NOD 1      EKV. SYST. GER  $L_i$ :na

$\sum_i(t) = \text{ANTAL } i \text{ SYSTEM } i$

$$\frac{\lambda_i}{c_i \mu_i} < 1$$

ALLA  $i$



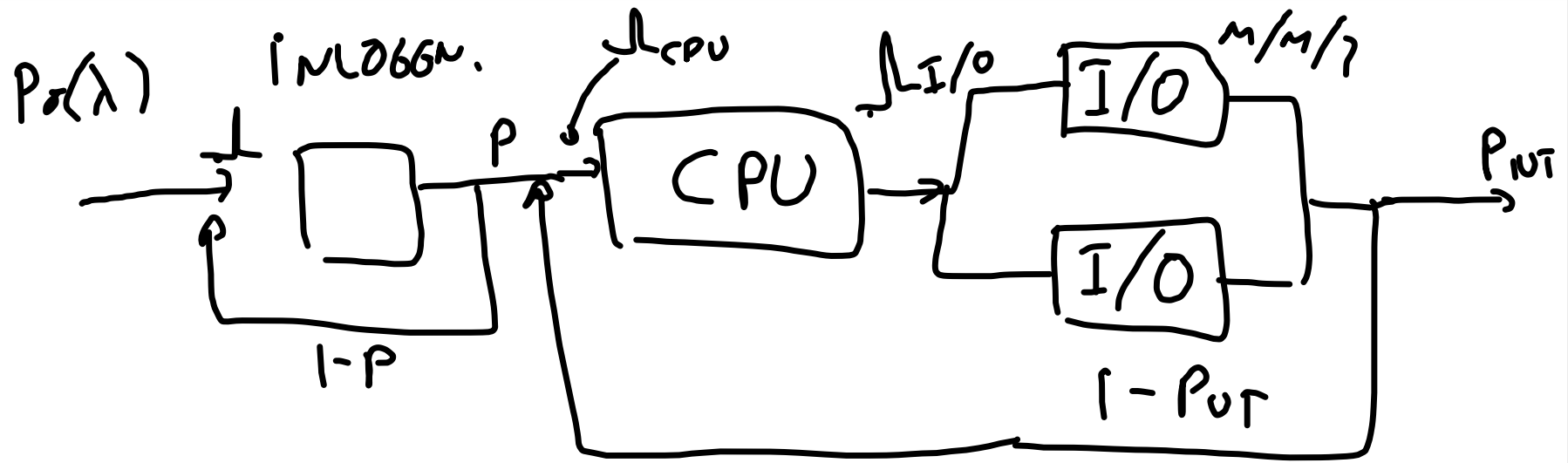
Es: POISSON-PROZESSE  
 INNE I JACKSON-  
 NATVERKET.

$$\lambda = \lambda + (1-p)\lambda$$

$$\lambda = \frac{\lambda}{p} \quad \text{for } p = \frac{1}{2}$$

$$\lambda = 2\lambda$$

$$\rho = \frac{\lambda}{1 \cdot \mu} = \frac{2\lambda}{\mu} < 1$$



$$\lambda_{LOGIN} = \lambda + (1-P)\lambda_{LOGIN} \quad \lambda_{LOGIN} = \frac{\lambda}{P}$$

$$\lambda_{CPU} = P\lambda_{LOGIN} + (1-P_{OUT}) \frac{\lambda_{I/O}}{\lambda_{CPU}}$$

$$\lambda_{I/O} = \lambda_{CPU}$$