Section: 10 Functional Analysis

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On certain series of quantum bounded symmetric domains

This work is carried out with my scientific supervisor L.Vaksman and is devoted to non-commutative complex analysis in bounded symmetric domains [1] of type C_n .

For this homogeneous space of the quantum group $Sp(n,\mathbb{R})$ the following results are received:

- existence and uniqueness for faithful irreducible *-representation of quantum polynomial algebra is proved;
- existence and uniqueness (up to scalar) of $U_q \mathfrak{sp}_n$ -invariant integral is established;
- explicit formulas for the Bergman and Cauchy-Szegö kernels are found;
- a quantum analogue of Borel embedding is obtained.

A great deal of these results hold for general quantum bounded symmetric domains (see [2]).

References

- L. Vaksman (ed), Lectures on q-analogues of Cartan domains and associated Harish-Chandra modules, arXiv:math.QA/0109198.
- [2] S. Sinel'shchikov, L. Vaksman, "On q-analogues of bounded symmetric domains and Dolbeault complexes", *Mathematical Physics, Analysis and Geometry*; Kluwer Academic Publishers, 1 (1998), 75–100, q-alg 9703005.

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