ON THE SPACE OF CURVATURE TENSORS OF A MANIFOLD WITH GRASSMANN STRUCTURE

N. Bokan, P. Matzeu and Z. Rakić

Abstract

We study the vector space of curvature tensors, $\mathcal{R}(G)$, of torsion free connections with holonomy group $G = GL(p, \mathbb{R}) \otimes GL(q, \mathbb{R})$, which is naturally connected with the study of the geometry and topology of manifolds with Grassmann structure. The complete decomposition of $\mathcal{R}(G)$ under the action of Gis obtained. The highest weight vectors are provided. It was shown that the Weyl projective curvature tensor has more complicated algebraic structure than in the cases of $GL(n, \mathbb{R})$ being a holonomy group. This decomposition imply a lot of geometrical properties (in the framework of transformation groups, harmonic normalization, half-flat Grassmann connections, etc.). We consider also the same problem for the vector space of covariant derivative of curvature tensors.

Key Words: holonomy group, space of curvature tensors, Grassmann manifold, Grassmann connection, normalization, torsion-free connection, action of a group, simple *G*-modules.

Mathematical Subject Classification 2000: 53C29, 53C30, 22E47

Affiliation of authors:

Neda Bokan

Faculty of Mathematics, University of Belgrade, Studentski trg 16, PP 550, 11001 Belgrade, Serbia, e-mail:neda@matf.bg.ac.yu

Paola Matzeu Dipartimento di Matematica, Viale Merello 92, 09123 Cagliari, Italy, e-mail:matzeu@vaxca1.unica.it

Zoran Rakić

Faculty of Mathematics, University of Belgrade, Studentski trg 16, PP 550, 11001 Belgrade, Serbia, e-mail:zrakic@matf.bg.ac.yu