

Large tridiagonal or banded linear systems appear in many applications, such as finite elements, difference schemes to differential equations, power distribution systems, etc. Two of the most popular parallel algorithms for solving tridiagonal systems are the Partition algorithm [4] and the Cyclic Reduction (CR) algorithm [1]. These algorithms are suitable especially for massively parallel computers.

The generalized Partition algorithm for banded linear systems is considered in [3] and generalized Block CR algorithm is considered in [7].

In the present work we compare the parallel implementations of the Partition algorithm and the CR algorithm in the cases of tridiagonal and banded linear systems.

The applied programming model could be named as Single Program Multiple Data paradigm and it is based on the most popular library for Message Passing Interface (MPI). The above mentioned algorithms are compared for different system dimensions and changing the configuration of parallel systems in terms of physical processors. The experimental results consider two factors for performance evaluation of parallel solutions: Parallel speedup and Efficiency.

Let us note that in our experiments was taken in advance the stability analysis in [2, 5, 6, 7].

References

- [1] R. Hockney and C. Jesshope, *Parallel Computers 2*, Adam Hilger, Bristol, 1988.
- [2] V. Pavlov, Stability of a parallel partitioning algorithm for special classes of banded linear systems, *Lecture Notes in Computer Science*, (Eds. L. Vulkov, J. Wasniewski et. al.), Springer, 1988 (2000), 658–665.
- [3] V. Pavlov and P. Yalamov, Stability issues of the Wang’s partitioning algorithm for banded and tridiagonal linear systems, *Lecture Notes in Computer Science*, (Eds. M. Dayde, I. Duff et. al.), Springer, 1685 (1999), 1149–1152.
- [4] H. Wang, A parallel method for tridiagonal linear systems, *ACM Transactions on Mathematical Software*, 7 (1981), 170–183.
- [5] P. Yalamov, On the stability of the cyclic reduction without back substitution for tridiagonal systems, *BIT*, 34 (1994), 428–447.
- [6] P. Yalamov and V. Pavlov, On the stability of a partitioning algorithm for tridiagonal systems, *SIAM J. Matrix Anal. Appl.*, v. 20, N 1 (1999), 159–181.
- [7] P. Yalamov and V. Pavlov, Stability of the block cyclic reduction, *Linear Algebra and Its Applications*, 249 (1996), 341–358.