We prove that for every rooted, finitely branching tree T of height ω without terminal nodes and for every finite weakly embedded subtree A of T, there is a finite list of equivalence relations $\{\mathbb{E}_i : 1 \leq i \leq T_n\}$ on $Em^A(T)$, where $Em^A(T)$ is the set of all finite weakly embedded subtrees of T which have the same embedding type as A, such that for every other equivalence relation $\mathbb{E}$ on $Em^A(T)$ there is a perfect strongly embedded subtree S of T and an equivalence relation $\mathbb{E}_i$ from the list such that

$$\mathbb{E} \restriction Em^A(S) \;=\; \mathbb{E}_i \restriction Em^A(S).$$