

7.3.42.

$$L\left\{\sin t U\left(t - \frac{\pi}{2}\right)\right\}$$

$$f(t) = \sin t U\left(t - \frac{\pi}{2}\right) =$$

$$\begin{aligned} & u = t - \frac{\pi}{2}, \quad \sin t = \sin\left(u + \frac{\pi}{2}\right) = \\ = & \sin u \cos \frac{\pi}{2} + \sin \frac{\pi}{2} \cos u = \cos u = \cos\left(t - \frac{\pi}{2}\right) = \end{aligned}$$

$$= \cos\left(t - \frac{\pi}{2}\right) U\left(t - \frac{\pi}{2}\right)$$

$$L\{f(t)\} = L\left\{\cos\left(t - \frac{\pi}{2}\right)U\left(t - \frac{\pi}{2}\right)\right\} =$$

$$= \left\{L\{g(t - a)U(t - a)\} = e^{-sa}L\{g(t)\}\right\} =$$

$$= e^{-s\frac{\pi}{2}}L\{\cos t\} = e^{-s\frac{\pi}{2}}\frac{s}{s^2 + 1}$$