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Miura transformation for the KP and mKP equations and solution of the (2+1) KN equationWe consider two dimensional Miura transformation

$$v(x, y, t) = -u_x(x, y, t) - u^2(x, y, t) - \sigma \partial_x^{-1} u_y(x, y, t) \quad (1)$$

which connects the solutions of the modified Kadomtsev-Petviashvili equation

$$M(u) = u_t + \frac{1}{4} u_{xxx} - \frac{3}{2} \left(u^2 u_x + \sigma u_x \partial_x^{-1} u_y - \frac{1}{2} \sigma^2 \partial_x^{-1} u_{yy} \right) = 0. \quad (2)$$

with the solutions of the Kadomtsev-Petviashvili equation

$$K(v) = \left(v_t + \frac{1}{4} v_{xxx} + \frac{3}{2} v v_x \right)_x + \sigma^2 \frac{3}{4} v_{yy} = 0. \quad (3)$$

We obtain the scheme of integration of (2) by the dressing method, which allows us to construct the solutions v of the KP and u of the system connected by the Miura transformation (1). The KP and mKP equations have not a wide set of explicit solutions. We present some new examples of plane soliton-like solutions of mKP (solitons on the moving background). It turns out that the family of solutions of the mKP equation corresponds to one and the same solution of the KP equation. Moreover, under the construction of the scheme of the integration of the mKP equation, the (2+1) generalization of the Krichever-Novikov equation

$$2\rho_x + \sigma \frac{\alpha_y}{\alpha_x} + \frac{\alpha_{xx}}{\alpha_x} = 0 \quad (4)$$

$$\alpha_t - 2\alpha_{xxx} - 3\sigma\alpha_{xy} + \frac{3!}{2}\sigma^2 \frac{\alpha_y^2}{\alpha_x} - \frac{3}{2} \frac{\alpha_{xx}^2}{\alpha_x} - \frac{3}{2} \sigma \rho_y = 0. \quad (5)$$

is arising by the natural way. The formulas for α and ρ based on the solution of the Marchenko integral equation are also obtained. 2000 MSC: 35Q51,

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