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Symmetric designs and strongly regular graphs constructed from the group $\mathrm{PSp}(4,3)$

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Abstract

We present a symmetric $(45,12,3)$ design, two symmetric $(40,13,4)$ designs, and a symmetric $(36,15,6)$ design constructed from the symplectic group $\mathrm{PSp}(4,3)$ defining an incidence relation on the conjugacy classes of the maximal subgroups. Incidence matrices of these designs are adjacency matrices of strongly regular graphs with parameters $(45,12,3,3)$, $(40,12,2,4)$ and $(36,15,6,6)$, respectively. The group $\mathrm{PSp}(4,3)$ acts transitively on the constructed designs and the corresponding strongly regular graphs.

Key words: symmetric design, strongly regular graph, symplectic group, automorphism group.

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