Package 'AID'

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Type Package

Title Box-Cox Power Transformation

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Author Osman Dag [aut, cre], Ozgur Asar [aut], Ozlem Ilk [aut]

Maintainer Osman Dag <osman.dag@hacettepe.edu.tr>

Description Performs Box-Cox power transformation for different purposes, graphical approaches, assesses the success of the transformation via tests and plots, computes mean and confidence interval for back transformed data.

License GPL (>= 2)

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AID-package   *Box-Cox Power Transformation*

Description

Performs Box-Cox power transformation for different purposes, graphical approaches, assesses the success of the transformation via tests and plots, computes mean and confidence interval for back transformed data.

Details

Package:	AID
Type:	Package
License:	GPL (>=2)

AADT   *Average Annual Daily Traffic Data*

Description

Average annual daily traffic data collected from the Minnesota Department of Transportation data base.

Usage

```
data(AADT)
```

Format

A data frame with 121 observations on the following 8 variables.

aadt average annual daily traffic for a section of road

ctypop population of county

lanes number of lanes in the section of road

width width of the section of road (in feet)

control a factor with levels: 1 = access control; 2 = no access control

class a factor with levels: 1 = rural interstate; 2 = rural noninterstate; 3 = urban interstate; 4 = urban noninterstate

truck availability situation of road section to trucks

locale a factor with levels: 1 = rural; 2 = urban, population <= 50,000; 3 = urban, population > 50,000

References

Cheng, C. (1992). Optimal Sampling for Traffic Volume Estimation, Unpublished Ph.D. dissertation, University of Minnesota, Carlson School of Management.

Neter, J., Kutner, M.H., Nachtsheim, C.J.,Wasserman, W. (1996). *Applied Linear Statistical Models (4th ed.)*, Irwin, page 483.

Examples

```
library(AID)

data(AADT)
attach(AADT)
hist(aadt)
out <- boxcoxfr(aadt, class)
confInt(out)
```

---

boxcoxfr   *Box-Cox Transformation for One-Way Independent Groups Designs*

Description

boxcoxfr performs Box-Cox transformation for one-way independent groups designs. It is useful to use if the normality or/and the homogenity of variance is/are not satisfied while comparing two or more groups.

Usage

```
boxcoxfr(y, x, option = "both", lambda = seq(-3, 3, 0.01), lambda2 = NULL,
  tau = 0.05, alpha = 0.05, verbose = TRUE)
```

Arguments

y	a numeric vector of data values.
x	a vector or factor object which gives the group for the corresponding elements of y.
option	a character string to select the desired option for the objective of transformation. "norm" and "var" are the options which search for a transformation to satisfy the normality of groups and the homogeneity of variances, respectively. "both" is the option which searches for a transformation to satisfy both the normality of groups and the homogeneity of variances. Default is set to "both".
lambda	a vector which includes the sequence of feasible lambda values. Default is set to (-3, 3) with increment 0.01.
lambda2	a numeric for an additional shifting parameter. Default is set to lambda2 = 0.
tau	the feasible region parameter for the construction of feasible region. Default is set to 0.05. If tau = 0, it returns the MLE of transformation parameter.

| alpha | the level of significance to check the normality and variance homogenity after transformation. Default is set to alpha = 0.05. |
| verbose | a logical for printing output to R console. |

Details

Denote y the variable at the original scale and y' the transformed variable. The Box-Cox power transformation is defined by:

$$y' = \begin{cases} \frac{y^\lambda - 1}{\lambda} \text{ , if } \lambda \neq 0 \\ log(y) \text{ , if } \lambda = 0 \end{cases}$$

If the data include any nonpositive observations, a shifting parameter λ_2 can be included in the transformation given by:

$$y' = \begin{cases} \frac{(y+\lambda_2)^\lambda - 1}{\lambda} \text{ , if } \lambda \neq 0 \\ log(y + \lambda_2) \text{ , if } \lambda = 0 \end{cases}$$

Maximum likelihood estimation in feasible region (MLEFR) is used while estimating transformation parameter. MLEFR maximizes the likehood function in feasible region constructed by Shapiro-Wilk test and Bartlett's test. After transformation, normality of the data in each group and homogeneity of variance are assessed by Shapiro-Wilk test and Bartlett's test, respectively.

Value

A list with class "boxcoxfr" containing the following elements:

method	method applied in the algorithm
lambda.hat	the estimated lambda
lambda2	additional shifting parameter
shapiro	a data frame which gives the test results for the normality of groups via Shapiro-Wilk test
bartlett	a matrix which returns the test result for the homogenity of variance via Bartlett's test
alpha	the level of significance to assess the assumptions.
tf.data	transformed data set
x	a factor object which gives the group for the corresponding elements of y
y.name	variable name of y
x.name	variable name of x

Author(s)

Osman Dag, Ozlem Ilk

References

Dag, O., Ilk, O. (2017). An Algorithm for Estimating Box-Cox Transformation Parameter in ANOVA. *Communications in Statistics - Simulation and Computation*, **46:8**, 6424–6435.

Examples

```
library(AID)

data(AADT)
attach(AADT)
out <- boxcoxfr(aadt, class)
out$shapiro
out$bartlett
out$tf.data
confInt(out, level = 0.95)


data <- rnorm(120, 10, 1)
factor <- rep(c("X", "Y", "Z"), each = 40)
out <- boxcoxfr(data, factor, lambda = seq(-5, 5, 0.01), tau = 0.01, alpha = 0.01)
confInt(out, level = 0.95)
```

---

boxcoxlm	*Box-Cox Transformation for Linear Models*

Description

boxcoxlm performs Box-Cox transformation for linear models and provides graphical analysis of residuals after transformation.

Usage

```
boxcoxlm(x, y, method = "lse", lambda = seq(-3,3,0.01), lambda2 = NULL, plot = TRUE,
   alpha = 0.05, verbose = TRUE)
```

Arguments

x	a nxp matrix, n is the number of observations and p is the number of variables.
y	a vector of response variable.
method	a character string to select the desired method to be used to estimate Box-Cox transformation parameter. To use Shapiro-Wilk test method should be set to "sw". For method = "ad", boxcoxnc function uses Anderson-Darling test to estimate Box-Cox transformation parameter. Similarly, method should be set to "cvm", "pt", "sf", "lt", "jb", "mle", "lse" to use Cramer-von Mises, Pearson Chi-square, Shapiro-Francia, Lilliefors and Jarque-Bera tests, maximum likelihood

estimation and least square estimation, respectively. Default is set to method = "lse".

lambda   a vector which includes the sequence of candidate lambda values. Default is set to (-3,3) with increment 0.01.

lambda2   a numeric for an additional shifting parameter. Default is set to lambda2 = 0.

plot   a logical to plot histogram with its density line and qqplot of residuals before and after transformation. Defaults plot = TRUE.

alpha   the level of significance to assess the normality of residuals after transformation. Default is set to alpha = 0.05.

verbose   a logical for printing output to R console.

Details

Denote y the variable at the original scale and y' the transformed variable. The Box-Cox power transformation is defined by:

$$y' = \begin{cases} \frac{y^\lambda - 1}{\lambda} = \beta_0 + \beta_1 x_1 + ... + \epsilon \text{ , if } \lambda \neq 0 \\ log(y) = \beta_0 + \beta_1 x_1 + ... + \epsilon \text{ , if } \lambda = 0 \end{cases}$$

If the data include any nonpositive observations, a shifting parameter λ_2 can be included in the transformation given by:

$$y' = \begin{cases} \frac{(y+\lambda_2)^\lambda - 1}{\lambda} = \beta_0 + \beta_1 x_1 + ... + \epsilon \text{ , if } \lambda \neq 0 \\ log(y + \lambda_2) = \beta_0 + \beta_1 x_1 + ... + \epsilon \text{ , if } \lambda = 0 \end{cases}$$

Maximum likelihood estimation and least square estimation are equivalent while estimating Box-Cox power transformation parameter (Kutner et al., 2005). Therefore, these two methods return the same result.

Value

A list with class "boxcoxlm" containing the following elements:

method   method preferred to estimate Box-Cox transformation parameter

lambda.hat   estimate of Box-Cox Power transformation parameter based on corresponding method

lambda2   additional shifting parameter

statistic   statistic of normality test for residuals after transformation based on specified normality test in method. For mle and lse, statistic is obtained by Shapiro-Wilk test for residuals after transformation

p.value   p.value of normality test for residuals after transformation based on specified normality test in method. For mle and lse, p.value is obtained by Shapiro-Wilk test for residuals after transformation

alpha   the level of significance to assess normality of residuals

tf.y   transformed response variable

tf.residuals   residuals after transformation

y.name   response name

x.name   x matrix name

Author(s)

Osman Dag, Ozlem Ilk

References

Asar, O., Ilk, O., Dag, O. (2017). Estimating Box-Cox Power Transformation Parameter via Goodness of Fit Tests. *Communications in Statistics - Simulation and Computation*, **46:1**, 91–105.

Kutner, M. H., Nachtsheim, C., Neter, J., Li, W. (2005). *Applied Linear Statistical Models. (5th ed.)*. New York: McGraw-Hill Irwin.

Examples

```
library(AID)

trees=as.matrix(trees)
boxcoxlm(x = trees[,1:2], y = trees[,3])
```

---

boxcoxnc	*Box-Cox Transformation for Normality of a Univariate Variable*

Description

`boxcoxnc` performs Box-Cox transformation for normality of a univariate variable and provides graphical analysis.

Usage

```
boxcoxnc(data, method = "sw", lambda = seq(-3,3,0.01), lambda2 = NULL, plot = TRUE,
  alpha = 0.05, verbose = TRUE)
```

Arguments

data	a numeric vector of data values.
method	a character string to select the desired method to be used to estimate Box-Cox transformation parameter. To use Shapiro-Wilk test method should be set to "sw". For method = "ad", boxcoxnc function uses Anderson-Darling test to estimate Box-Cox transformation parameter. Similarly, method should be set to "cvm", "pt", "sf", "lt", "jb", "ac", "mle" to use Cramer-von Mises, Pearson Chi-square, Shapiro-Francia, Lilliefors, Jarque-Bera tests, artificial covariate method and maximum likelihood estimation, respectively. Default is set to method = "sw".
lambda	a vector which includes the sequence of candidate lambda values. Default is set to (-3,3) with increment 0.01.
lambda2	a numeric for an additional shifting parameter. Default is set to lambda2 = 0.

plot	a logical to plot histogram with its density line and qqplot of raw and trans-formed data. Defaults plot = TRUE.
alpha	the level of significance to check the normality after transformation. Default is set to alpha = 0.05.
verbose	a logical for printing output to R console.

Details

Denote y the variable at the original scale and y' the transformed variable. The Box-Cox power transformation is defined by:

$$y' = \begin{cases} \frac{y^\lambda - 1}{\lambda} & \text{, if } \lambda \neq 0 \\ log(y) & \text{, if } \lambda = 0 \end{cases}$$

If the data include any nonpositive observations, a shifting parameter λ_2 can be included in the transformation given by:

$$y' = \begin{cases} \frac{(y+\lambda_2)^\lambda - 1}{\lambda} & \text{, if } \lambda \neq 0 \\ log(y + \lambda_2) & \text{, if } \lambda = 0 \end{cases}$$

Value

A list with class "boxcoxnc" containing the following elements:

method	method preferred to estimate Box-Cox transformation parameter
lambda.hat	estimate of Box-Cox Power transformation parameter based on corresponding method
lambda2	additional shifting parameter
statistic	statistic of normality test for transformed data based on specified normality test in method. For artificial covariate method, statistic is obtained by Shapiro-Wilk test for transformed data
p.value	p.value of normality test for transformed data based on specified normality test in method. For artificial covariate method, p.value is obtained by Shapiro-Wilk test for transformed data
alpha	the level of significance to assess normality.
tf.data	transformed data set
var.name	variable name

Author(s)

Osman Dag, Ozgur Asar, Ozlem Ilk

References

Asar, O., Ilk, O., Dag, O. (2017). Estimating Box-Cox Power Transformation Parameter via Good-ness of Fit Tests. *Communications in Statistics - Simulation and Computation*, **46:1**, 91–105.

Dag, O., Asar, O., Ilk, O. (2014). A Methodology to Implement Box-Cox Transformation When No Covariate is Available. *Communications in Statistics - Simulation and Computation*, **43:7**, 1740–1759.

Examples

```
library(AID)

data(textile)

out <- boxcoxnc(textile[,1], method = "sw")
out$lambda.hat # the estimate of Box-Cox parameter based on Shapiro-Wilk test statistic
out$p.value # p.value of Shapiro-Wilk test for transformed data
out$tf.data # transformed data set
confInt(out) # mean and confidence interval for back transformed data


out2 <- boxcoxnc(textile[,1], method = "sf")
out2$lambda.hat # the estimate of Box-Cox parameter based on Shapiro-Francia test statistic
out2$p.value # p.value of Shapiro-Francia test for transformed data
out2$tf.data
confInt(out2)
```

---

confInt.boxcoxfr   *Mean and Confidence Interval for Back Transformed Data*

Description

confInt.boxcoxfr calculates mean and confidence interval for back transformed data in each group and plots their error bars with confidence intervals.

Usage

```
## S3 method for class 'boxcoxfr'
confInt(x, level = 0.95, plot = TRUE, xlab = NULL, ylab = NULL, title = NULL,
  width = NULL, verbose = TRUE, ...)
```

Arguments

x	a boxcoxfr object.
level	the confidence level.
plot	a logical to plot error bars with confidence intervals.
xlab	a label for the x axis, defaults to a description of x.

ylab	a label for the y axis, defaults to a description of y.
title	a main title for the plot.
width	a numeric giving the width of the little lines at the tops and bottoms of the error bars (defaults to 0.15).
verbose	a logical for printing output to R console.
...	additional argument(s) for methods.

Details

Confidence interval in each group is constructed separately.

Value

A matrix with columns giving mean, lower and upper confidence limits for back transformed data. These will be labelled as (1 - level)/2 and 1 - (1 - level)/2 in % (by default 2.5% and 97.5%).

Author(s)

Osman Dag

Examples

```
library(AID)

data(AADT)
attach(AADT)
out <- boxcoxfr(aadt, class)
confInt(out, level = 0.95)
```

---

confInt.boxcoxnc   *Mean and Confidence Interval for Back Transformed Data*

Description

confInt is a generic function to calculate mean and confidence interval for back transformed data.

Usage

```
## S3 method for class 'boxcoxnc'
confInt(x, level = 0.95, verbose = TRUE, ...)
```

Arguments

x	a boxcoxnc object.
level	the confidence level.
verbose	a logical for printing output to R console.
...	additional argument(s) for methods.

Value

A matrix with columns giving mean, lower and upper confidence limits for back transformed data. These will be labelled as (1 - level)/2 and 1 - (1 - level)/2 in % (by default 2.5% and 97.5%).

Author(s)

Osman Dag

Examples

```
library(AID)

data(textile)
out <- boxcoxnc(textile[,1])
confInt(out) # mean and confidence interval for back transformed data
```

---

grades   *Student Grades Data*

Description

Overall student grades for a class thaught by Dr. Ozlem Ilk

Usage

```
data(grades)
```

Format

A data frame with 42 observations on the following variable.

grades a numeric vector for the student grades

Examples

```
library(AID)

data(grades)
hist(grades[,1])
out <- boxcoxnc(grades[,1])
confInt(out, level = 0.95)
```

---

textile   *Textile Data*

Description

Number of Cycles to Failure of Worsted Yarn

Usage

```
data(textile)
```

Format

A data frame with 27 observations on the following variable.

textile a numeric vector for the number of cycles

References

Box, G. E. P., Cox, D. R. (1964). An Analysis of Transformations (with discussion). *Journal of the Royal Statistical Society, Series B (Methodological)*, **26**, 211–252.

Examples

```
library(AID)

data(textile)
hist(textile[,1])
out <- boxcoxnc(textile[,1])
confInt(out)
```

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