

5.81

State i - # units of water in the dam
(at the beginning of the month)

$$i = 0, 1, 2, 3$$

Decision k = # units of water that should
be released during the month

$$k = 0, 1, 2, 3$$

Transition matrices

$$P(k) = \{p_{ij}(k)\}$$

release no units ($k=0$):

$$\begin{matrix} i \backslash j & 0 & 1 & 2 & 3 \\ 0 & 1/6 & 1/3 & 1/3 & 1/6 \\ 1 & 0 & 1/6 & 1/3 & 1/2 \\ 2 & 0 & 0 & 1/6 & 5/6 \\ 3 & 0 & 0 & 0 & 1 \end{matrix} = P(0)$$

← if it contains more than 3 units of water
excess water is released

release 1 unit ($k=1$)

$$\begin{matrix} i \backslash j & 0 & 1 & 2 & 3 \\ 0 & - & - & - & - \\ 1 & 1/6 & 1/3 & 1/3 & 1/6 \\ 2 & 0 & 1/6 & 1/3 & 1/2 \\ 3 & 0 & 0 & 1/6 & 5/6 \end{matrix} = P(1)$$

← $k > i$ cannot release water we
do not have.

$$\begin{pmatrix} - & - & - & - \\ 1/6 & 1/3 & 1/3 & 1/6 \\ 0 & 1/6 & 1/3 & 1/2 \end{pmatrix} = P(2)$$

$$\begin{pmatrix} - & - & - & - \\ - & - & - & 5/6 \\ 1/6 & 1/3 & 1/3 & 1/6 \end{pmatrix} = P(3)$$